

## **Forming Equations – page 2**

- 1-  $4x + 10$ ; length is 12 cm
- 2-  $5x + 120 = 360$ ; angle is 58 degrees
- 3-  $12x + 18$ ;  $12x + 18 = 48$ ; £2.50 and £5.50

## **Rearranging Difficult Formulae – page 3**

- 1-  $c = v - 2a - 3b$
- 2-  $t = \frac{A}{\pi+5}$
- 3-  $s = \frac{R-2t}{3+\pi}$
- 4-  $l = \frac{km}{1+k}, m = \frac{l+kl}{k}$
- 5-  $x = \frac{4A-5k}{k}$
- 6-  $u = \frac{u^2-Rv}{kR-1}$
- 7-  $y = \frac{30x+20}{3-3x}$
- 8-  $a = 80b^2 + 3$
- 9-  $y = \sqrt{\frac{s^2}{4\pi^2d^2}}$

## **Factorisation – page 4**

- 1-
  - a)  $2(x + 2)$
  - b)  $2(y + 5)$
  - c)  $3(x + 4)$
  - d)  $3(x - 2)$
  - e)  $5(x - 3)$
- 2-
  - a)  $p(p + 7)$
  - b)  $x(x + 4)$
  - c)  $y(y - 2)$
  - d)  $p(p - 5)$
  - e)  $x(x + 1)$
- 3-
  - a)  $2x(x + 3)$
  - b)  $2y(y - 4)$
  - c)  $5p(p + 2)$
  - d)  $7c(c - 3)$
  - e)  $3x(2x + 3)$
- 4-
  - a)  $2x(x - 2y)$
  - b)  $2t(t + 5u)$
  - c)  $2x(3x - 4y)$
  - d)  $3xy(xy + 3)$

### Difference of two squares - page 5

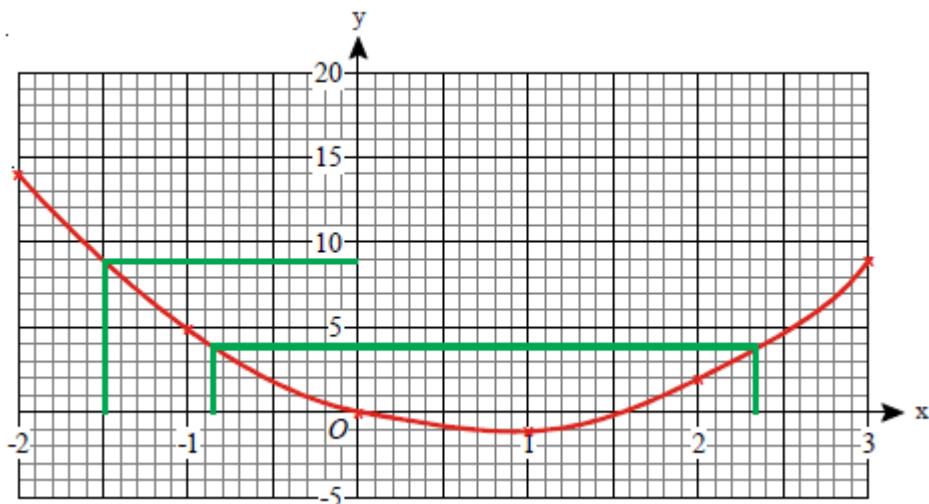
- 1-  $(x - 4)(x + 4), (a - b)(a + b), (y - 3)(y + 3), (x - 1)(x + 1), (x - 0.5)(x + 0.5), (x - \frac{1}{3})(x + \frac{1}{3})$
- 2-  $(x - 2y)(x + 2y), (3a^2 - b)(3a^2 + b), (3x - 4y)(3x + 4y), (0.25x - y)(0.25x + y), (x - \frac{1}{3}y)(x + \frac{1}{3}y)$
- 3-  $\frac{5(y-2)}{y+5}, \frac{3(2x-1)}{x-2}, \frac{4x}{3x-2}, \frac{5a+4b}{2b}$

### Algebraic Fractions – page 6

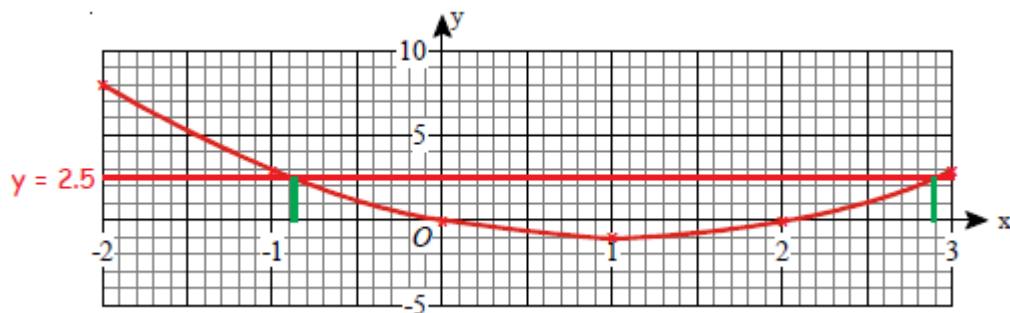
- 1-  $\frac{3}{7x}, 2xy, 9a^2, \frac{2(x+3)}{5}, \frac{1-7b^2}{3ab^2}$
- 2-  $\frac{x}{x+5}, \frac{x}{x+4}$
- 3-  $\frac{3x+1}{2x-3}$
- 4-  $\frac{9}{2x}, \frac{11}{12x}, \frac{7x-1}{10}, \frac{x-7}{(x+2)(2x+1)}$
- 5-  $2/3, -2 \text{ or } 6, 2.5 \text{ or } 6, -0.5 \text{ or } 1.5, 2.75, x = 0 \text{ or } 3$

### Drawing quadratics – page 7

- 1-  $y = 9, x = -0.85 \text{ or } 2.33$



- 2-  $x = -0.89 \text{ or } 2.9$



### **Solving quadratic Equations by factorising - page 8**

1-

- a)  $x = -2$  or  $-3$
- b)  $x = -4$  or  $-5$
- c)  $x = -3$  or  $2$
- d)  $x = -8$  or  $3$
- e)  $x = 2$  or  $4$
- f)  $x = -7$  or  $-4$
- g)  $x = -3$  or  $-1/2$
- h)  $x = -3/2$  or  $-1/3$
- i)  $x = -5$  or  $2/3$
- j)  $x = 7/3$  or  $9$

2- yes,  $x = -1$

3- yes,  $x = -5$

### **Solving quadratic Equations by factorising - page 9**

1.  $-0.268$  or  $-3.732$
2.  $-0.838$  or  $-7.16$
3.  $-0.562$  or  $3.56$
4.  $0.298$  or  $6.70$
5.  $-3.16$  or  $0.158$
6.  $-2.27$  or  $2.94$
7.  $-7.5$  or  $21.5$
8.  $-1.70$  or  $7.11$
9.  $13.0$
10.  $-2.19$  or  $3.19$

### **Completing the Square - page 10**

1. Proof
2. Proof
3. 2 and 6
4. 3 and 8
5. 3 and 9;  $-9$
6. 4 and  $-21$ ;  $(4, -21)$
7. 25 and 5;  $25$ ;  $x = 5$

### **Simultaneous Equations With a Quadratic - page 11**

1.  $(3, 3)$  and  $(-2, -2)$
2.  $(-1, -3)$  and  $(4, 12)$
3.  $(5, 7)$  and  $(-3, -1)$
4.  $(6, -1)$  and  $(1, -5)$
5. No points of intersection;  $(1.4, -4.8)$  and  $(4, 3)$

**Quadratic Inequalities - page 12**

1.  $-4 < x < -2$
2.  $x < -7; 5 < x$
3.  $2 \leq x \leq 7$
4.  $x < -5; 6 < x$
5.  $x < -8; 4 < x$
6.  $x < -10; -2 < x$
7.  $x < -2.5; -2 < x$
8.  $8/7 \leq x \leq 2$
9.  $0.5 \leq x \leq 6$
10.  $x < -15; 10 < x$

**Proof - page 13**

1. Proof
2. Proof
3. Proof
4. Proof
5. Proof
6. Proof

**Trigonometry - page 14**

1. 22.2
2. 11.6
3. 27.8
4. 64.2
5. 27.9

**Bearings by trigonometry - page 15**

1. 0.52.2 and 232.2
2. 19.1

**Sine and Cosine rules - page 16**

1. 36.2
2. 6.30
3. 109.6
4. 13.9 and 11.3

**Area of Triangles - page 17**

1. 26.8
2. 106
3. 356

**3-D coordinates - page 18**

1. (5,3,0)
2. (5,0,0)
3. (5,0,4)
4. (0,0,4)
5. (0,3,0)

**Pythagoras in 3D - page 19**

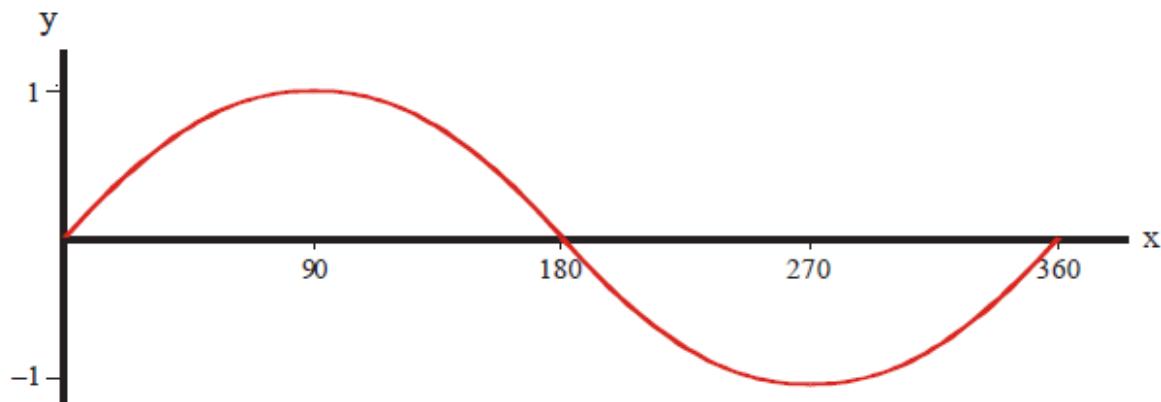
1. 7.81
2. 11.8
3. 27.4
4. 5.5

**Trigonometry in 3D - page 20**

1. 17.1
2. 55.9 and 26.6

**Graphs of Trigonometric Functions - page 21-22**

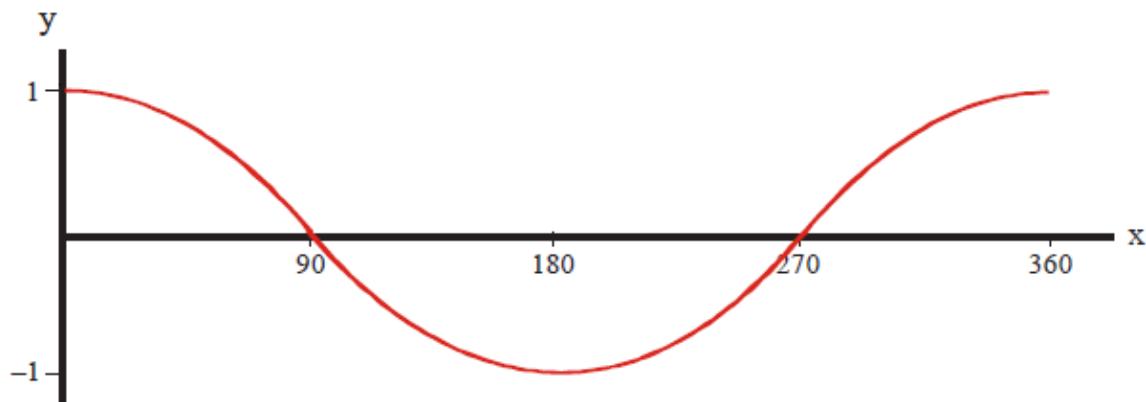
1.



Given that  $\sin 30^\circ = 0.5$ , write down the value of:

- (i)  $\sin 150^\circ$     0.5
- (ii)  $\sin 330^\circ$     -0.5

2.

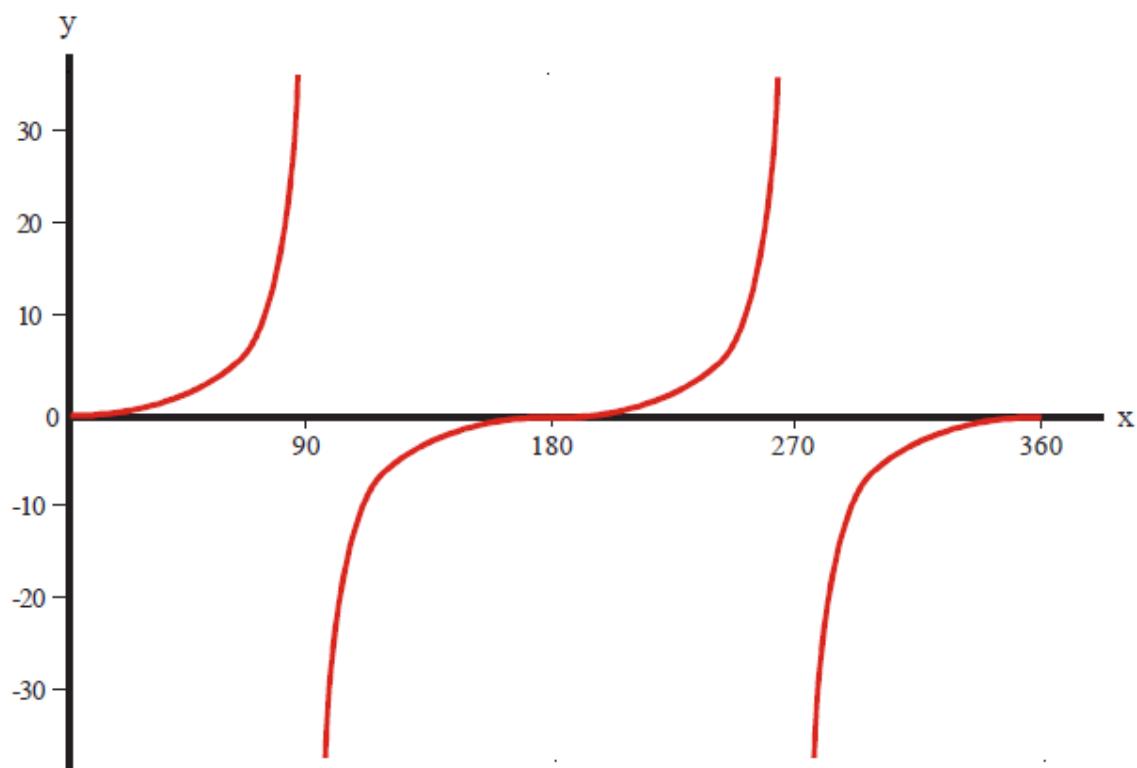


Given that  $\cos 60^\circ = 0.5$ , write down the value of:

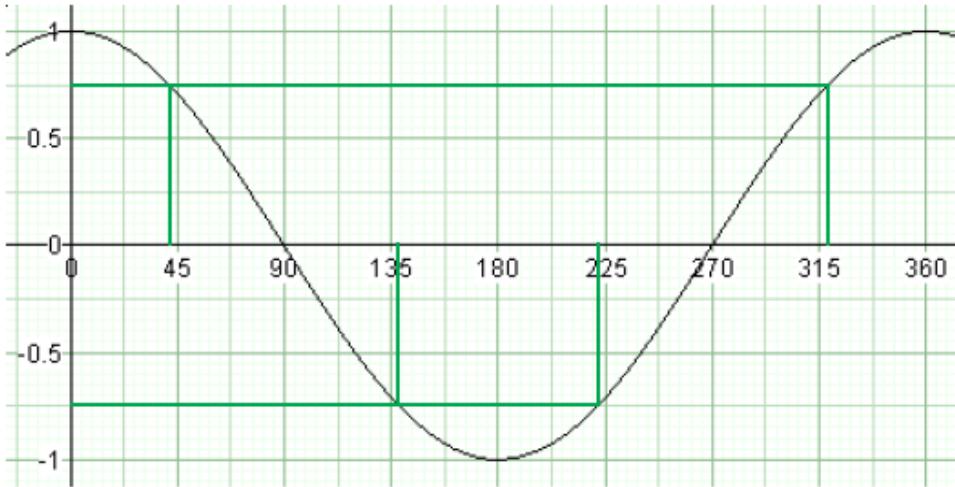
(i)  $\cos 120^\circ$  **-0.5**

(ii)  $\cos 240^\circ$  **-0.5**

3.



4.



- a) Use the graph to solve  $\cos x = 0.75$  for  $0 \leq x \leq 360^\circ$      $x = 41^\circ$  and  $319^\circ$   
b) Use the graph to solve  $\cos x = -0.75$  for  $0 \leq x \leq 360^\circ$      $x = 138^\circ$  and  $221^\circ$

### Transformations of graphs – page 23

- 1-  $(4, -1); (1, -6); (1, 1); (0.5, -1); y = x^2 - 2x$
- 2- Curve through the origin; stretch along the y-axis by a SF of 2.
- 3- U shaped parabola with vertex at  $(2, 3)$
- 4-  $V(-2, -5); -2 + \sqrt{5}$  and  $-2 - \sqrt{5}$

### Transformations of Trig Functions– page 24

- 1- Through the origin, periodicity of 180, asymptotes at 90, 270
- 2-  $A=2$ ,  $b=3$

### Iterations – page 25

- 1-  $7/16$
- 2- 2.669584272
- 3-  $-547/81; -6.561443673; -6.53541368$ ; approximate solutions to the equation

### Direct and Inverse Proportion– page 26

- 1-  $x = 7y; 7; 14; 70$
- 2-  $a = 48/b; 48; 6; 4.8; 12; 2; 15$
- 3- 2
- 4-  $p = 3q^2; 147; 3$
- 5-  $y = 4x^2; c = 16; n = -0.5$

## Surds – page 27

Please use your calculator to check your work

## Fractional and Negative Indices – page 28

1) Simplify

a)  $(p^5)^5$   $p^{25}$

c)  $x^5 \div x^2$   $x^3$

e)  $(m^5)^{-2}$   $m^{10}$

b)  $k^3 \times k^2$   $k^5$

d)  $(p^2)^{-3}$   $p^{-6}$

f)  $(3xy^2)^3$   $27x^3y^6$

2) Without using a calculator, find the exact value of the following.

a)  $4^0 \times 4^2$   $16$   
 $1 \times 16 = 16$

c)  $7^5 \div 7^3$   $49$   
 $7^2 = 49$

e)  $(8^5)^0$   $1$   
 $8^0 = 1$

b)  $5^4 \times 5^{-2}$   $25$   
 $5^2 = 25$

d)  $\frac{6^7}{6^6}$   $6$   
 $6^1 = 6$

f)  $(2^3)^2$   $64$   
 $2^6 = 64$

3) Work out each of these, leaving your answers as exact fractions when needed.

a)  $4^0$   $1$

e)  $4^{-2}$   $\frac{1}{16}$

i)  $49^{\frac{1}{2}}$   $7$

m)  $49^{-\frac{1}{2}}$   $\frac{1}{7}$

b)  $7^0$   $1$

f)  $8^{-1}$   $\frac{1}{8}$

j)  $32^{\frac{2}{5}}$   $4$

n)  $32^{-\frac{2}{5}}$   $\frac{1}{4}$

c)  $25^0$   $1$

g)  $5^{-3}$   $\frac{1}{125}$

k)  $27^{\frac{1}{3}}$   $3$

o)  $27^{-\frac{1}{3}}$   $\frac{1}{3}$

d)  $139^0$   $1$

h)  $10^{-5}$   $\frac{1}{100000}$

l)  $16^{\frac{3}{2}}$   $64$

p)  $16^{-\frac{3}{2}}$   $\frac{1}{64}$

4)  $5\sqrt{5}$  can be written in the form  $5^n$ .

Find the value of  $n$ .  $1.5$   $5^1 \times 5^{\frac{1}{2}}$

5)  $2 \times \sqrt{8} = 2^m$

Find the value of  $m$ .  $2.5$   $2^1 \times (2^3)^{\frac{1}{2}}$

6) Find the value of  $x$  when

$\sqrt{125} = 5^x$   $1.5$   $(5^3)^{\frac{1}{2}}$

7) Find the value of  $y$  when

$$\sqrt{128} = 2^y \quad 3.5 \quad (2^7)^{\frac{1}{2}}$$

8)  $a = 2^x, b = 2^y$

a) Express in terms of  $a$  and  $b$

i)  $2^{x+y}$  ii)  $2^{2x}$  iii)  $2^{x+2y}$   $ab^2$

$$ab = 16 \text{ and } 2ab^2 = 16$$

b) Find the value of  $x$  and the value of  $y$ .  $x = 5, y = -1$

$$16 = 2^x \times 2^y \quad 16 = 2(2^x \times 2^y \times 2^y)$$

$$= 2^{x+y} \quad 8 = 2^x \times 2^y \times 2^y$$

$$x + y = 4 \quad x + 2y = 3$$

### Equations of Circle and Loci – page 29

1. proof

2. proof

### Cubic and Reciprocal Functions– page 29

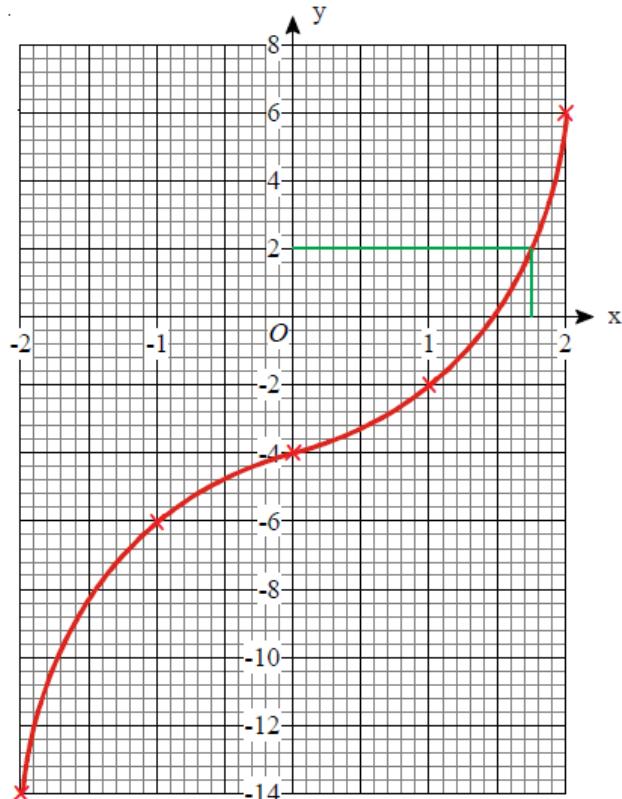
1) a) Complete this table of values for  $y = x^3 + x - 4$

x	-2	-1	0	1	2
y	-14	-6	-4	-2	6

b) On the grid, draw the graph of  $y = x^3 + x - 4$

c) Use the graph to find the value of  $x$  when  $y = 2$

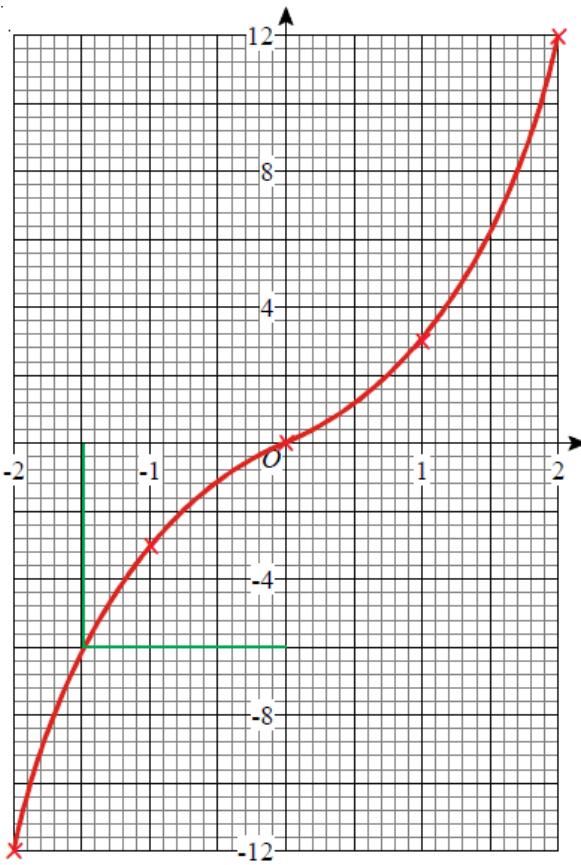
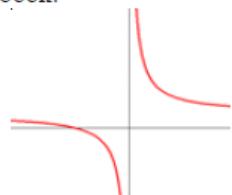
$$x = 1.75$$



- 2) a) Complete this table of values for  
 $y = x^3 + 2x$

x	-2	-1	0	1	2
y	-12	-3	0	3	12

- b) On the grid, draw the graph of  
 $y = x^3 + 2x$
- c) Use the graph to find the value  
of x when  $y = -6$   
 $x = -1.5$
- 3) Sketch the graph of  $y = 1 + \frac{1}{x}$   
in your book.



### Recognise the shapes of functions – page 31

$$y = 2^x; y = 2x^2 + 1; y = 3x^3; y = -2x^3$$

$$y = 5x - x^3; y = \frac{2}{x}; y = -\frac{2}{x}; y = 3x - 1$$

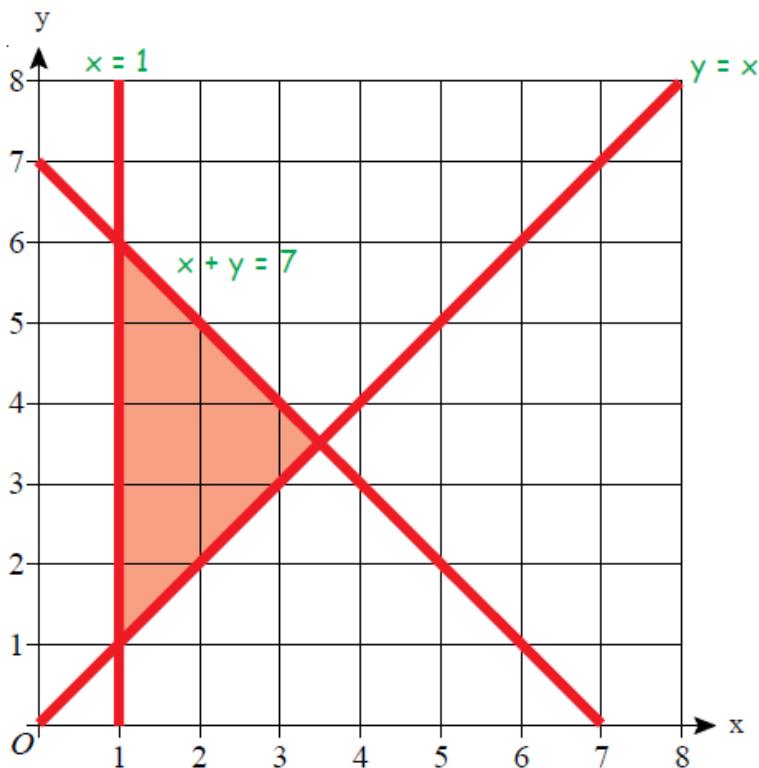
### Graphs of exponential functions– page 32

1-  $p = 0.6; q = 5$

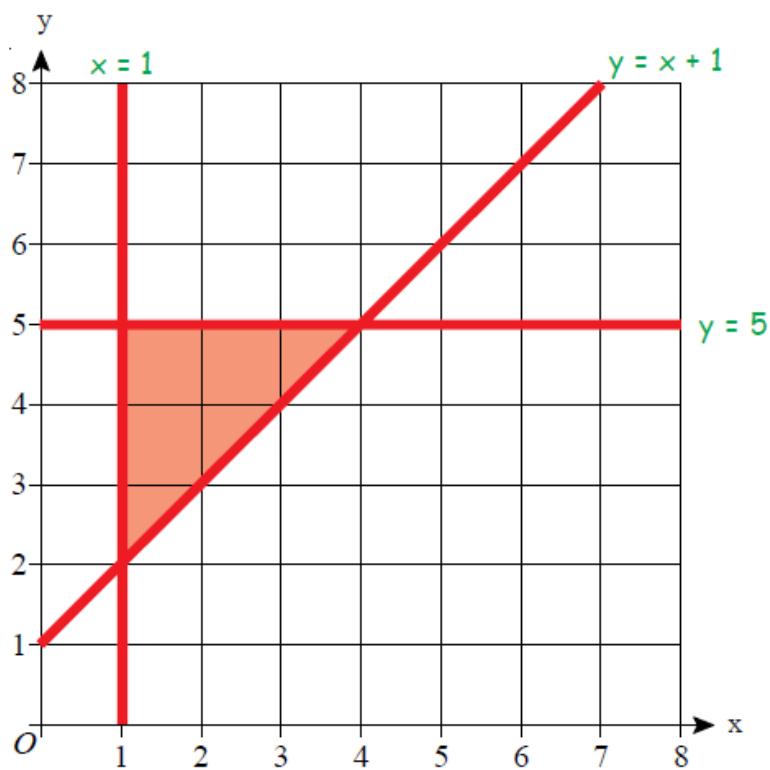
2- Draw a right-angle triangle of dimension  $y, x$  and  $y - 3$

**Region– page 33**

1.



2.



**Vectors - page 34-35**

1. Proof
2.  $k = 0.5$
3.  $k = 0.25$
4.  $k = 4$

**Vectors - page 36**

- 1-  $p+q; 2p$  vs.  $p$
- 2-  $3a - 3b; 9a$  vs.  $3a$

**Averages from a table - page 37**

- 1- 52; 2; 5
- 2- Explanation; 1.92
- 3-  $30 < t \leq 45$ ; 37

**Scatter Graphs - page 38**

- 1- Positive; round 14
- 2- Negative; close to 13.6

**Cumulative Frequency - page 39**

Plotting using the upper bounds; answers close to 34; 11.3; 8

**Box plots - page 40**

- 1- 19.5
- 2- Drawn accordingly

**Histograms - page 41**

- 1- Correct fd;
- 2- Table with 5; 12; 34 and 8

**Tree Diagrams - page 42**

1. 0.42
2.  $42/90$
3.  $36/56; 26/56; 30/56$
4.  $30/210; 108/210$

**And & Or Questions – page 43**

1.  $9/32$
2. 0.0036; 0.1128
3. 0.66

**Venn Diagrams – page 44**

1. 1/16
2. 4
3. 29